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PURE MATH

ALGEBRA AND FUNCTION

Level & Board	EDEXCEL (A-LEVEL)
ΤΟΡΙΟ:	QUADRATICS
PAPER TYPE:	SOLUTION 6
TOTAL QUESTIONS	8
TOTAL MARKS	38

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• (i) $3x^3 - 17x^2 - 6x = 0$ We can first factor out the common form of x $x(3x^2 - 17x - 6) = 0$ \Rightarrow x = 0 or $3x^2 - 17x - 6 = 0$ \Rightarrow Now, $3x^2 - 17x - 6 = 0$ Here a = 3, b = -17, c = -6Using quadratic formula $x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$ Plugging these values into the formula $\chi = \frac{-(-17)\pm\sqrt{(-17)^2 - 4}(3)(-6)}{2(3)}$ $x = \frac{17 \pm \sqrt{284 + 72}}{6}$ $x = \frac{17 \pm \sqrt{361}}{6}$ $x = \frac{17 \pm 19}{6}$ $x = \frac{17+19}{6}$ $x = \frac{17 - 19}{6}$ or $x = \frac{-2}{6}$ $x = \frac{36}{6}$ $x = \frac{-1}{2}$ x = 6

• Now, We have three solution for the equation $3x^3 - 17x^2 - 6x = 0$

$$x = 0, x = 6, x = \frac{-1}{3}$$

So, these are all the solutions to the given condition.

• (ii)
$$3(y-2)^6 - 17(y-2)^4 - 6(y-2)^2 = 0$$

Let
$$(y-2)^2 = x$$

 $\Rightarrow 3x^3 - 17x^2 - 6x = 0$
 $\Rightarrow x(3x^2 - 17x - 6) = 0$
 $x = 0$ or $3x^2 - 17x - 6 = 0$
But , Here
 $(y-2)^2 = 0$, $a = 3$, $b = -17$, $c = -6$
 $y-2 = 0$, using quadratic formula
 $y = 2$, $x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$
, $x = \frac{-(-17) \pm \sqrt{(17)^2 - 4(3)(-6)}}{2(3)}$
, $x = \frac{17 \pm \sqrt{36}}{6}$
, $x = \frac{17 \pm \sqrt{36}}{6}$
, $x = \frac{17 \pm 19}{6}$, $x = \frac{17 - 19}{6}$
, $x = 6$, $x = \frac{-1}{3}$
 $\Rightarrow (y-2)^2 = 6$, $(y-2)^2 = \frac{-1}{2}$
 $\Rightarrow \forall -2 = \pm \sqrt{6}$, However, since the square of a real

number

 $y-2=\pm\sqrt{6}$, cannot be negative a this equation has no

$$y-2=\pm\sqrt{6}$$
 , real solution for y.
and

$$y = 2 \pm \sqrt{6}$$

So, the real solutions for the original equation
$$3(y-2)^6 - 17(y-2)^4 - 6(y-2)^2 = 0$$

$$y = 2 + \sqrt{6}$$
 $Y = 2 - \sqrt{6}$ $Y = 2$

The discriminant is given by: Discriminant = 0 $b^2-4ac = 0$ But, the coefficient are a = k, b = k-3, c = 1

 $(k-3)^{2}-4(k)(1) = 0$ $k^{2} + 9 - 6k - 4k = 0$ $k^{2} - 10k + 9 = 0$ Factorization $k^{2} - 9k - k + 9 = 0$ K(k-9) - 1(k-9) = 0 (k-1)(k-9) = 0 $K - 1 = 0 , \quad k-9 = 0$ $K = 1 , \quad k = 9$

So, the possible values of k for the quadratic equation to have two equal real roots are: k = 9 and k = 1.



Substitute x = -4 into
$$kx^2 + (3k+1) \times 8 = 0$$

 $k(-4)^2 + (3k+1)(-4) - 8 = 0$
 \Rightarrow
 $16k - 12k - 4 - 8 = 0$
 $4k - 12 = 0$
 $4k = 12$
 $K = 3$

(b)

First we have the value of k, which is 4, So k=3 : By parts (a)

 \Rightarrow

$$kx^{2} + (3k+1) x+8=0$$

$$3x^{2} + 10x - 8 = 0$$
Factorization
$$3x^{2} + 12x - 2x - 8 = 0$$

$$3x(x+4) - 2(x+4) = 0$$

$$(3x-2)(x+4) = 0$$

$$3x-2=0 \text{ or } x+4 = 0$$

$$x = \frac{2}{3} \text{ or } x = -4$$
So, the second possible value of x is:
$$x = \frac{2}{3} \text{ and } x = -4$$

This equation is Based on the nature of roots.
Let
Equation is
$$ax^2 + bx + c = 0$$
 and the discriminant $= b^2$ - 4ac
If Discriminant $= 0$
Then equation has real roots.
 $b^2 - 4ac = 0$
Here, $a = k+3$, $b = 2(k+3)$, $c=4$
 $\Rightarrow [2(k+3)]^2 - 4[k+3] [4] = 0$
 $\Rightarrow 4(k+3)^2 - 16(k+3) = 0$
 $bividing by 4 \text{ on both side}$
 $(k+3)^2 - 4(k+3) = 0$
 $k^2 + 6k + 9 - 4k - 12 = 0$
 $k^2 + 2k - 3 = 0$ \therefore Factorize
 $k^2 + 3k - k - 3 = 0$
 $K(k+3) - 1(k+3) = 0$
 $(k+3)(k-1) = 0$
 $K = -3$, $k = 1$
But $k = -3$ not possible (Coefficient of $x^2 \pm 0$
so, value of $k = 1$.

Q.5

The quadratic equation is given

$$x^{2}-4x - 1 = 2p(x-5)$$

 $x^{2}-4x - 1 = 2px - 10p$
 $x^{2}-4x - 2px - 1 + 10p = 0$

$$\Rightarrow x^{2} + (-4-2p) + (10p-1) = 0$$
Here,
 $a - 1, b = -4-2p, c = 10p - 1$
Two equal root
 $b^{2} - 4ac = 0$
 $(-4 - 2p)^{2} - 4(1)(10p - 1) = 0$
 $16 + 16p + 4p^{2} - 40p + 4 = 0$
 $4p^{2} - 24p + 20 = 0$

$$\Rightarrow p^{2} - 6p + 5 = 0$$
Factorization
 $p^{2} - 5p - p + 5 = 0$
 $P(p - 5) - 1(p - 5) = 0$
 $(p - 1)(p - 5) = 0$
 $P - 1 = 0$ or $p - 5 = 0$
 $P = 1$ or $p = 5$
So,
 $P = 1 - 5$

Given

 $2qx^{2} + qx - 1 = 0$ For a quadratic equation, $ax^{2} + bx + c = 0$ The expression for solutions $x = \frac{-b \pm \sqrt{b^{2} - 4ac}}{2a}$

Where b^2 - 4ac is called discriminant.

(a) Since, given is a quadratic equation with no real roots, its discriminant must be:

q²+8q = 0 q(q + 8) = 0 q = 0 or q = -8 So, the critical points on curve for given condition are -8 and

0.

(b)

Therefore, conditions for q²+8q < 0 are: q > -8 q < 0 ⇒ -8 < q < 0

Q.7

$$4 - 3x - x^2$$

$$4 - (x^2 + 3x)$$

Complete the square coefficient of the x term: 3 divide it in half: $\frac{3}{2}$

Square it: $\left(\frac{3}{2}\right)^2$

Use
$$\left(\frac{3}{2}\right)^2$$
 to complete the square:
= $4 + \left(\frac{3}{2}\right)^2 - \left(x^2 + 3x + \left(\frac{3}{2}\right)^2\right)$
= $\frac{25}{4} - \left(x + \frac{3}{2}\right)^2$



$$x^{2} + 13x + 21 = 21 \quad or \quad x^{2} + 13x + 21 = -21$$

$$\Rightarrow \quad x^{2} + 13x + 21 - 21 = 0 \quad or \quad x^{2} + 13x + 21 + 21 = 0$$

$$\Rightarrow \quad x^{2} + 13x = 0 \quad or \quad x^{2} + 13x + 42 = 0$$

$$\Rightarrow \quad x(x + 13) = 0 \quad or \quad (x + 6)(x + 7) = 0$$

$$\Rightarrow \quad x = 0 \text{ and } x = -13 \quad or \quad x = -6 \text{ and } x = -7$$

$$S.S = \{-13, -7, -6, 0\}$$

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